

Work in Progress:  
Parameters of the Equilibrium Distribution Function  
for the NLED Reference Scenario

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# NLED Reference scenario

## Reference AUG pulse # 31213

- Energetic Particles from NBI
  - ▷ Passing Orbits
  - ▷ n, P show off axis profiles
- Rich Phenomenology (similarly seen in DIII-D and JT-60U)
  - ▷ e-GAMs
  - ▷ TAEs
  - ▷ RSAEs
- DATA for comparison and code validation
  - ▷ spectrograms
  - ▷ modal analysis
  - ▷ post processing analysis by transport codes

# Equilibrium Distribution Function

- Constants of Motion at leading order if  $B = \nabla\psi \times \nabla\phi + F\nabla\phi$ 
  - toroidal canonical momentum:  $\mathcal{P}_\phi = \psi + (F/\omega_c)v_{\parallel}$
  - energy:  $w = v^2/2 = v_{\parallel}^2/2 + \mu|B|$
  - $\lambda = \mu/w = (1 - v_{\parallel}^2/v^2)/|B|$ , being  $\mu = v_{\perp}^2/(2|B|)$

- Parameters

- ▷  $\mathcal{N}$  is the overall regularization factor
- ▷  $T_w, \alpha_w$  are the parameters of the *Gamma* distribution in energy (at fixed  $\lambda$ )
- ▷  $\mathcal{P}_{\phi 0}, \Delta_{P_\phi}$  are the parameters of the *Normal* distribution in  $\mathcal{P}_\phi$
- ▷  $\lambda_0, \Delta_\lambda$  are the parameters of the *Normal* distribution in  $\lambda$  (at fixed energy)
- ▷  $w_b, w_c$  are the parameters of the *SlowingDown* distribution in energy

$$f_{\text{Ref1}}(\mathcal{P}_\phi, w, \lambda) = \mathcal{N} \frac{(1 + \lambda/\lambda_0)(w/T_w)^{\alpha_w} \text{H}(w_b - w)}{\sqrt{2\pi} w^{3/2} + w_c^{3/2}} \times$$

$$\times \exp \left[ -\frac{(\mathcal{P}_\phi - \mathcal{P}_{\phi 0})^2}{\Delta_{P_\phi}^2} \right] \exp \left[ -\frac{w}{T_w} \left( \frac{\lambda - \lambda_0}{\Delta_\lambda} \right)^2 \right]$$

# First set of Parameters for the NLED REF Scenario

First estimate of the EDF parameters

- ▷  $\mathcal{N} = 1.2 \times 10^{17} \text{ m}^{-3}$ ,
- ▷  $T_w = 31.13 \text{ keV}$ ,
- ▷  $\alpha_w = 1.0$ ,
- ▷  $\mathcal{P}_{\phi 0} = 0.035 \text{ Wb}$ ,
- ▷  $\Delta_{P\phi} = 0.02 \text{ Wb}$
- ▷  $\lambda_0 = 0.08 \text{ T}^{-1}$
- ▷  $\Delta_\lambda = 0.12 \text{ T}^{-1}$
- ▷  $w_b = 93 \text{ keV}$ ,
- ▷  $w_c = 15 \text{ keV}$