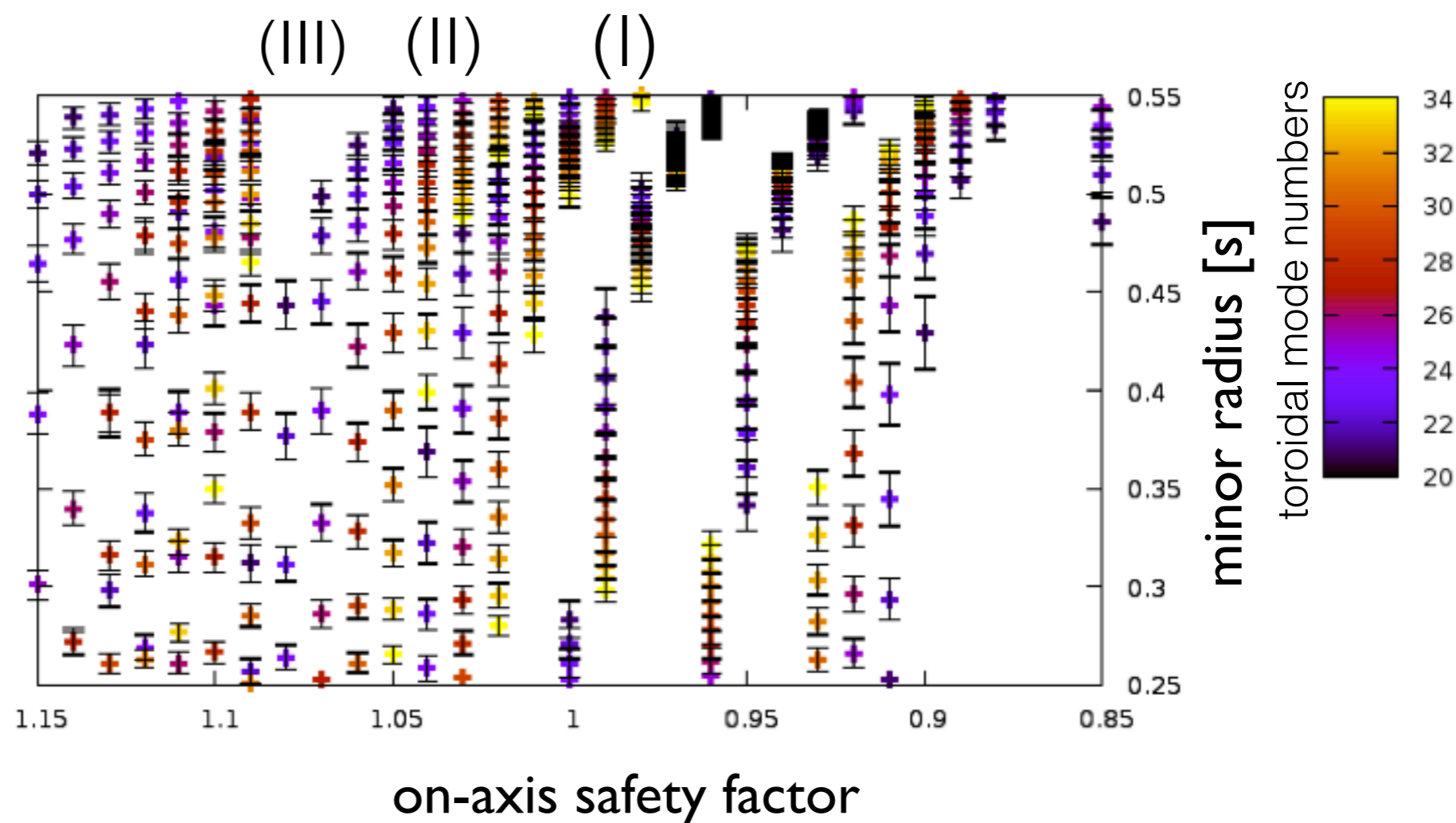


- degree of (non-linear) Alfvén eigenmode (AE) resonance overlap will determine the nature of EP transport [Berk 1995] in ITER and DEMO

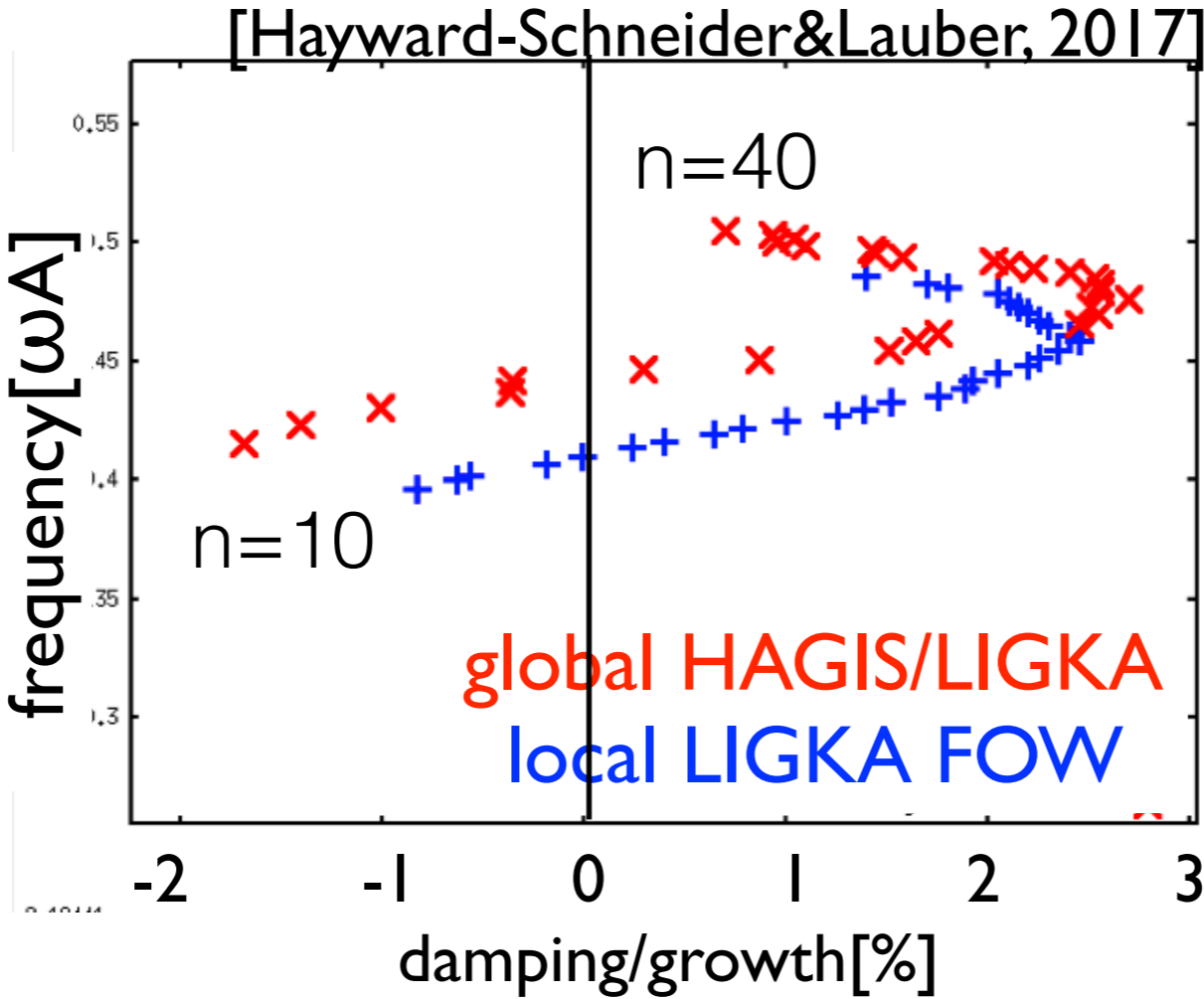
example: 15MA ITER
 scenario: linear TAE- α
 resonances depend strongly on q_0 :
 strongly overlapping (I),
 intermediate (II) and scarce
 (III) TAEs spectra can exist
 here: only linearly unstable
 modes are shown

(N.B: for small particle orbits, $P\varphi$ and s are similar, thus the radial mode overlap is a proxy for resonance overlap)



automated HAGIS/LIGKA workflow L2/L3/L4 for ITER 15 MA including FLR/FOW

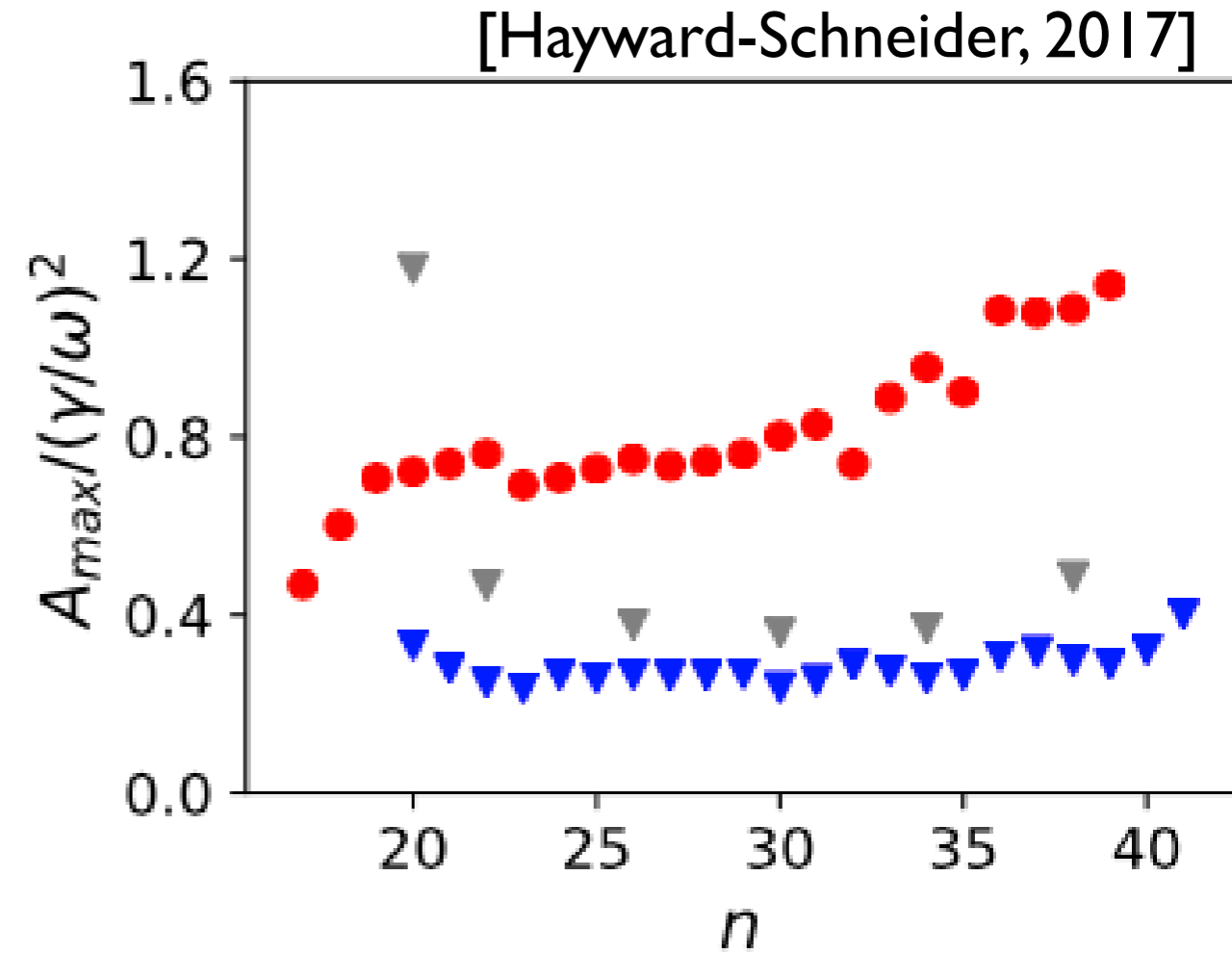
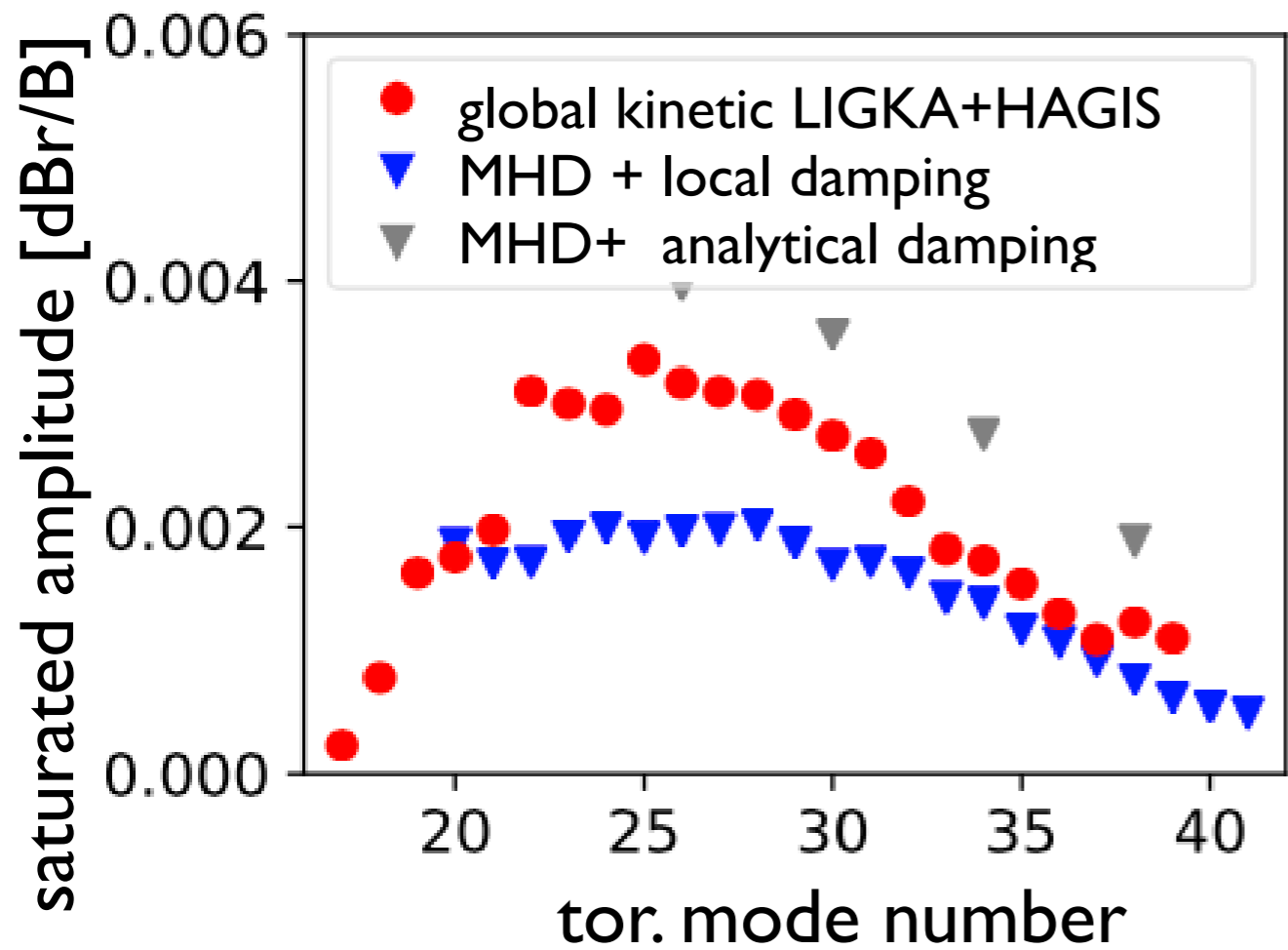
including some global information (k_r, k_\perp) in local model:



10-100 times faster than global solver: analytical finite orbit width version of LIGKA based on analytical theories [Zonca 1996/98]; benchmarked in relevant limit [Lauber 2018]:

reasonable agreement for intermediate and high mode numbers

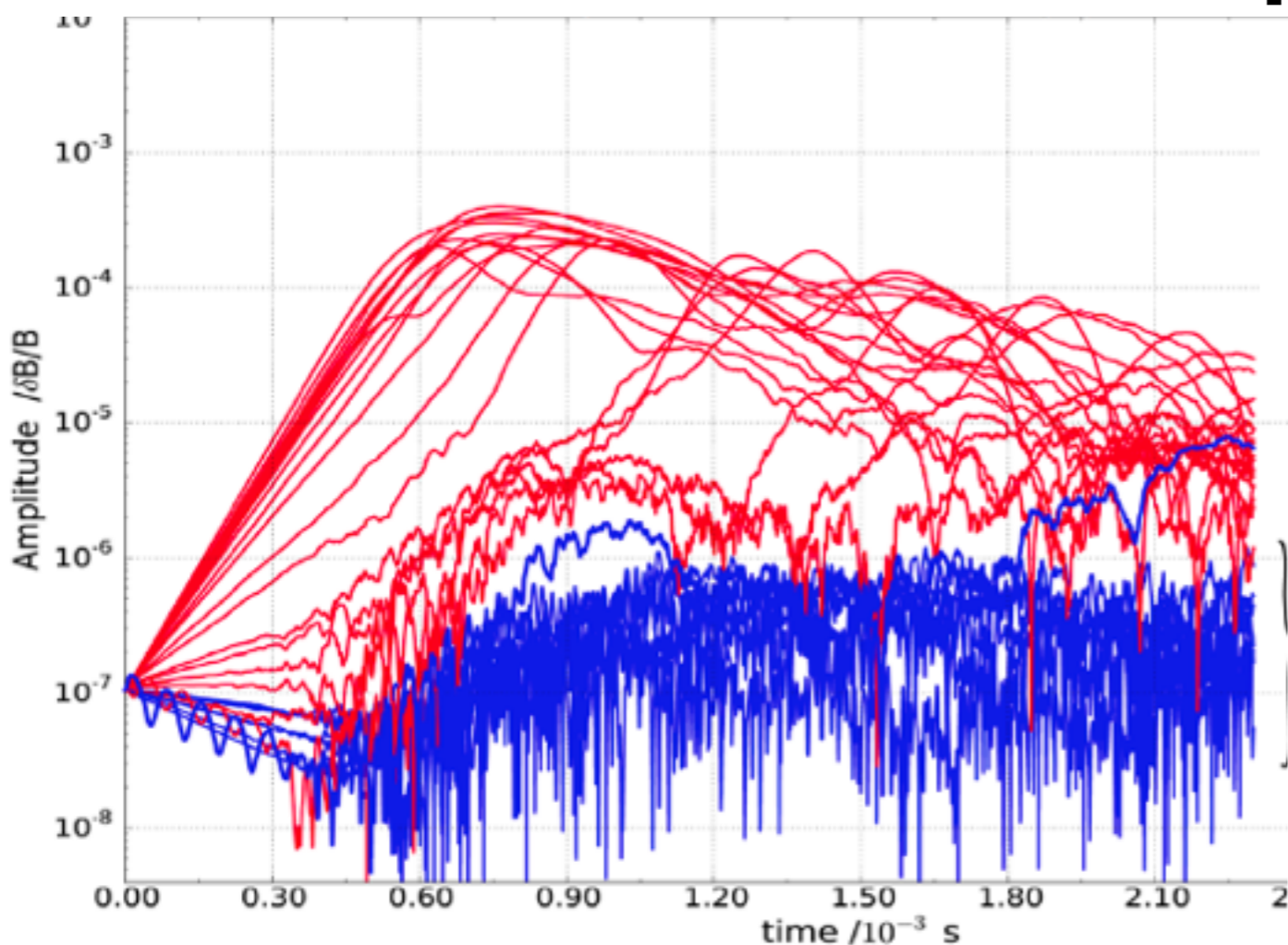
automated HAGIS/LIGKA workflow HI including FLR/FOW



runtime: minutes - few hours
 for whole range of mode numbers
 global effects crucial, non-perturbative features observed;
 no constant between $A \sim (\gamma/\omega)^2$

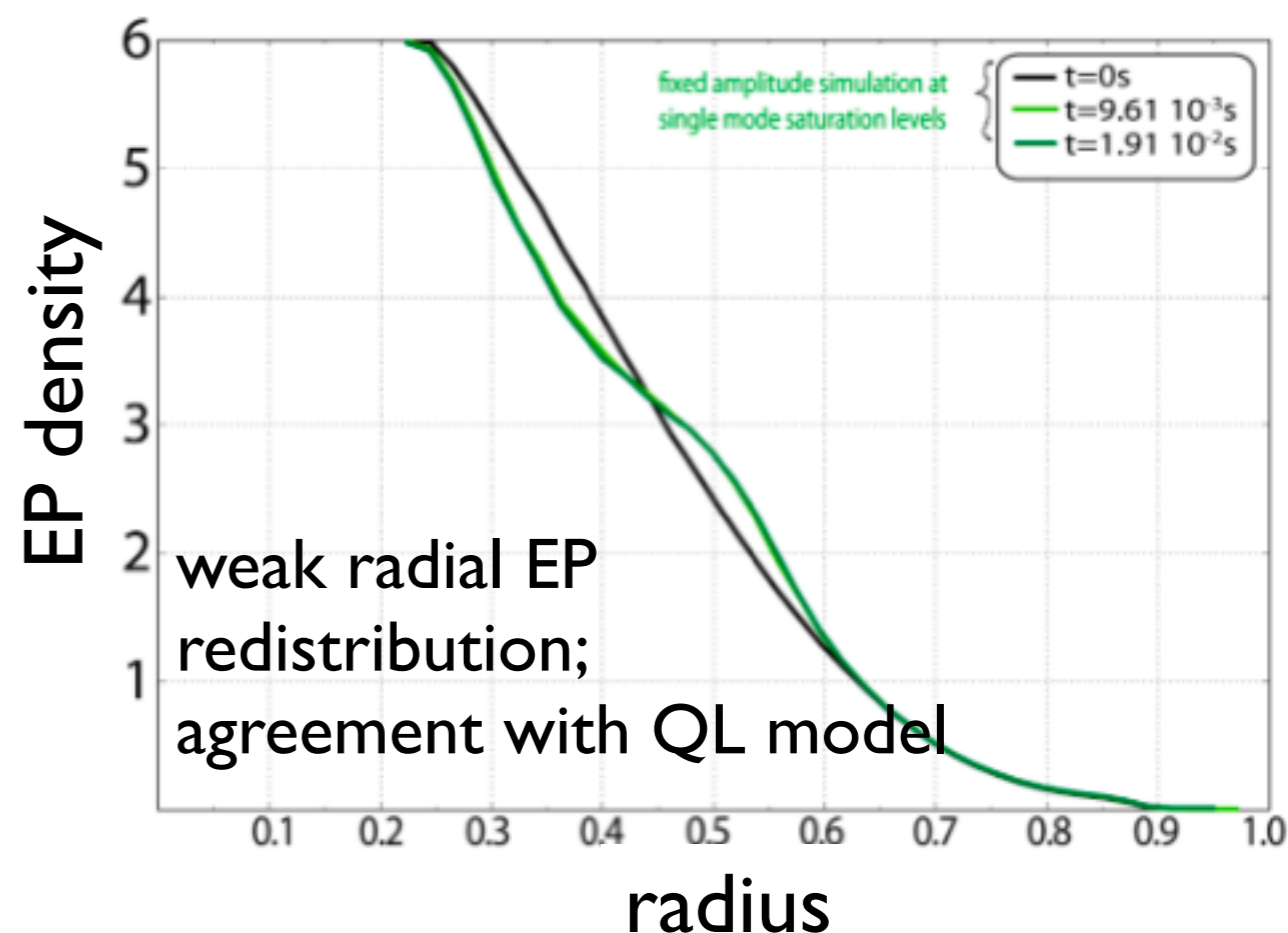
automated HAGIS/LIGKA workflow H2 including FLR/FOW

HAGIS/LIGKA model, ITER 15 MA TAEs [Schneller, 2015]



'sea' of weakly unstable TAEs expected with small EP transport; agreement with QL estimates

high-*n* branch in multi mode



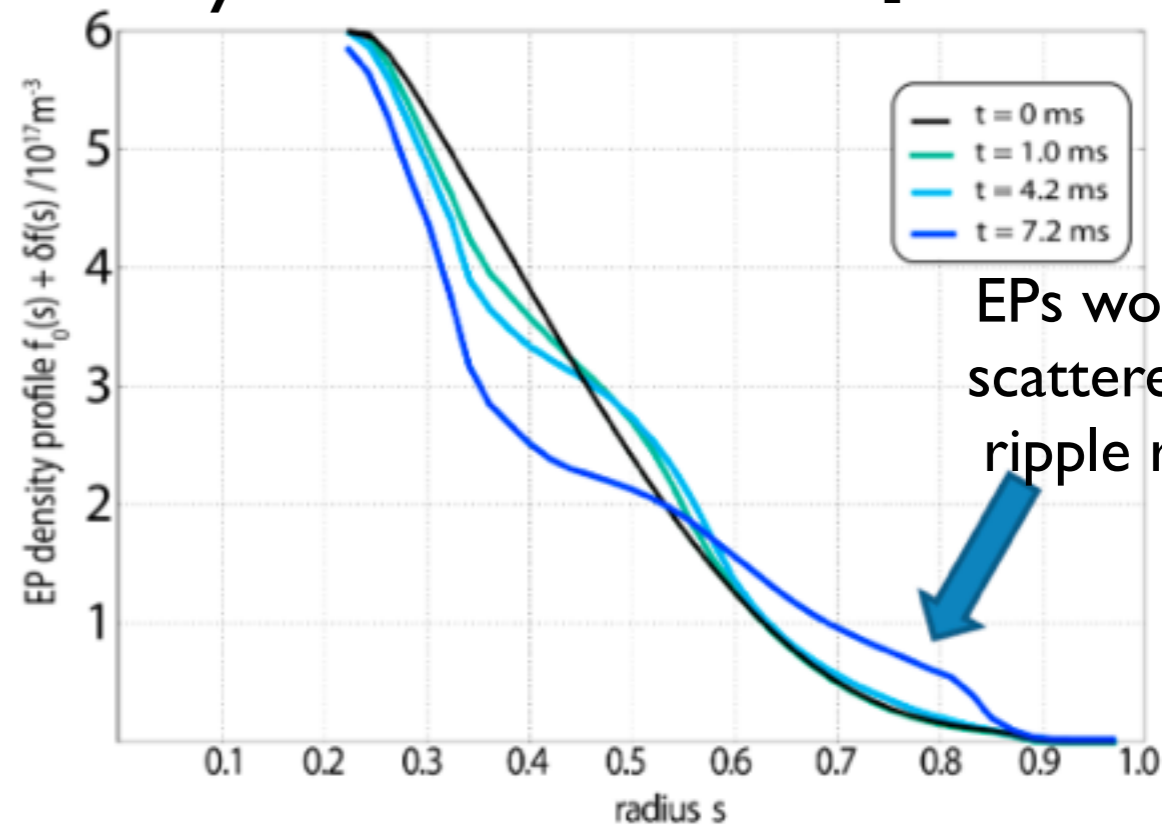
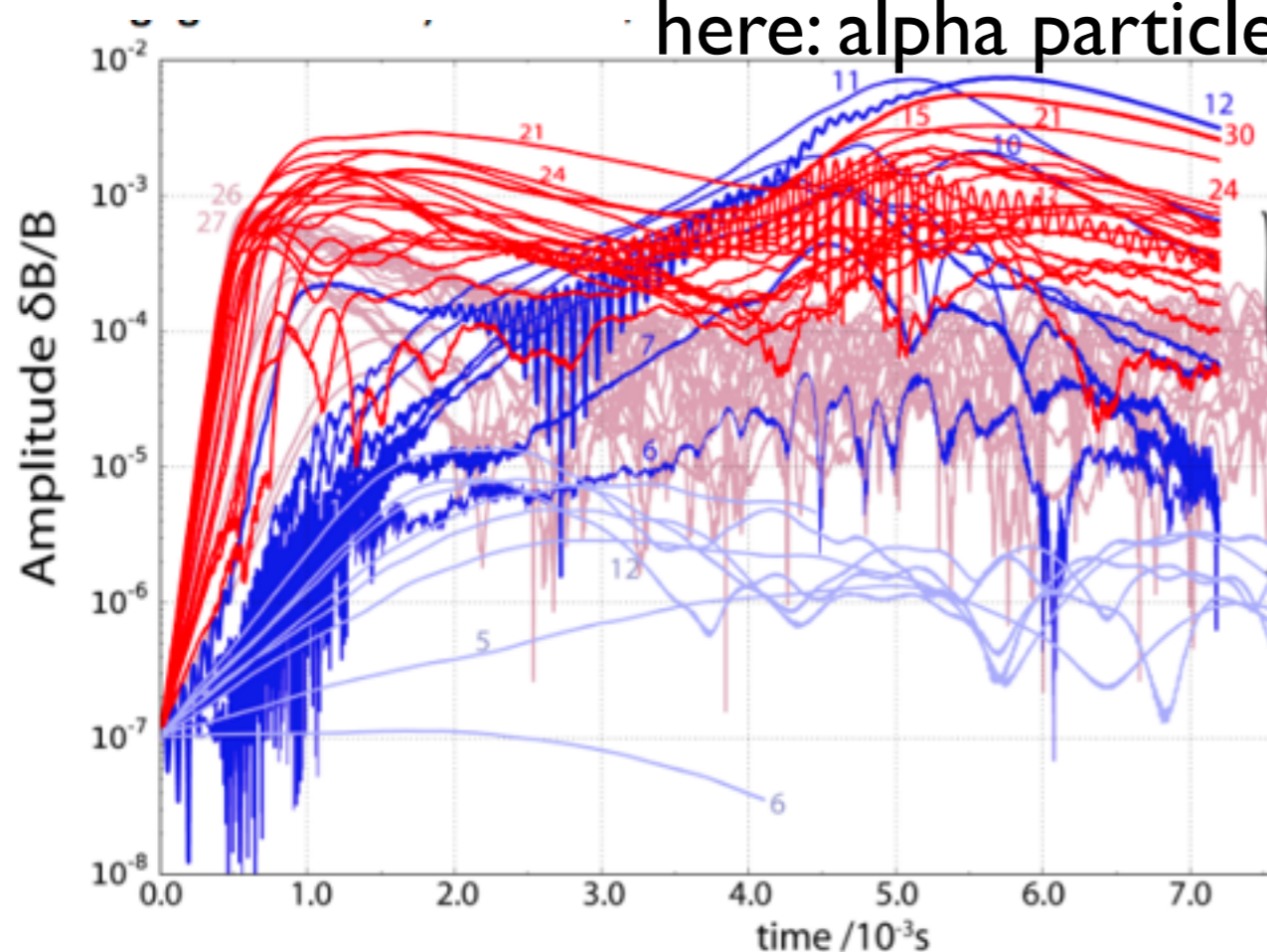
weak radial EP redistribution; agreement with QL model

check QL linear resonance broadening models [Berk, 1995] and reduced descriptions 1d beam plasma model [Carlevaro, 2015-17]

automated HAGIS/LIGKA workflow H2 including FLR/FOW

here: alpha particle density doubled!

[Schneller, 2015]



EPs would be scattered into ripple region

above simulations are 'worst case':

reduced amplitudes found when zonal flow dynamics is included (forced excitation)!

[Todo, 2011, Biancalani, 2016, Vlad 2017]

recently: similar behaviour found using global ORB5 [T. Hayward-Schneider, 2019]
(in contrast to other studies [M. Fitzgerald, 2015] not observing this transition)

the LIGKA model equations

can be evaluated numerically or analytically

$$0 = \sum_a e_a \int d^2v \{J_0 f\}_a + \nabla_{\perp} \cdot \frac{m_i n_i \nabla_{\perp} \phi}{B^2} \quad \text{QN}$$

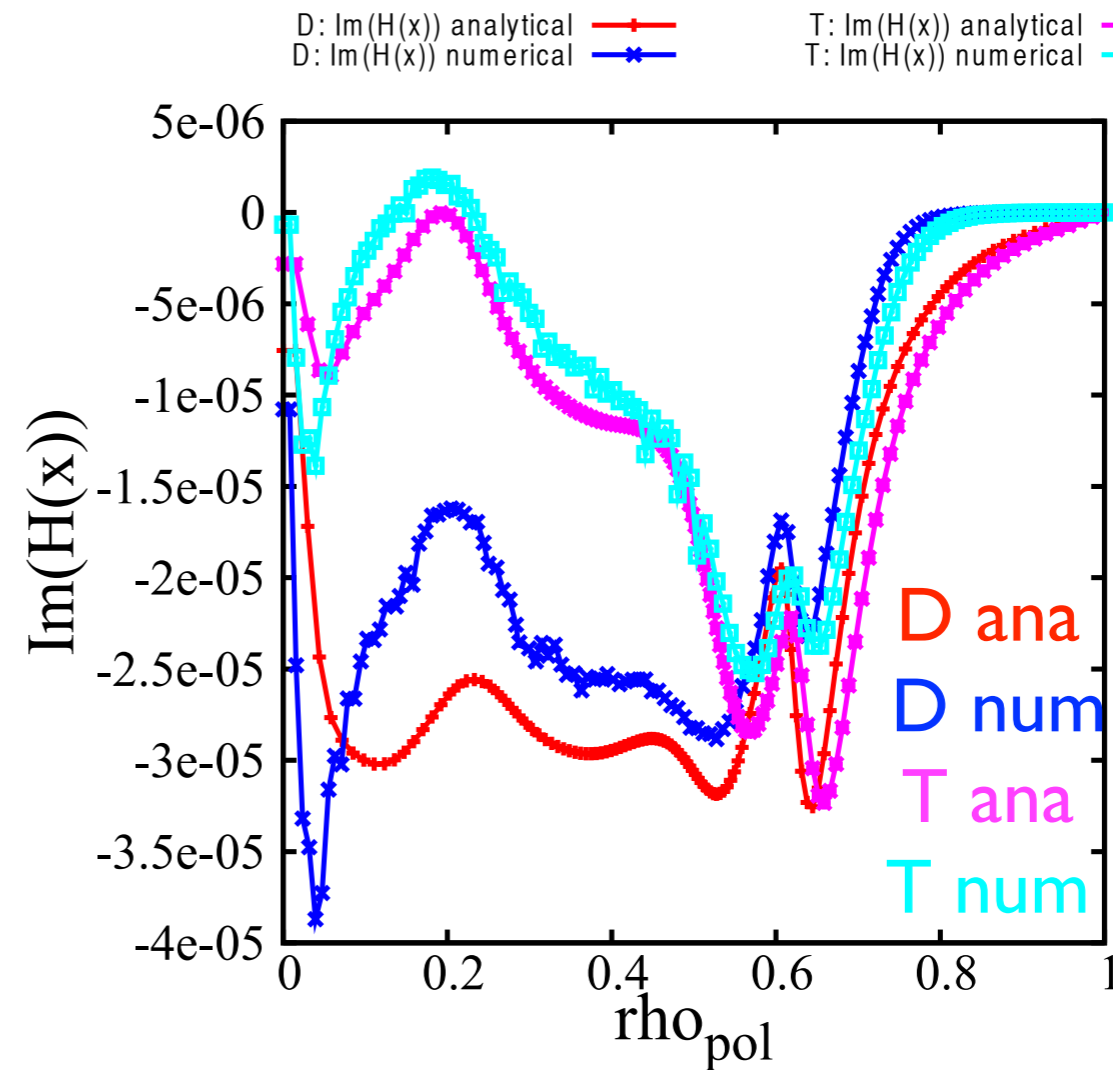
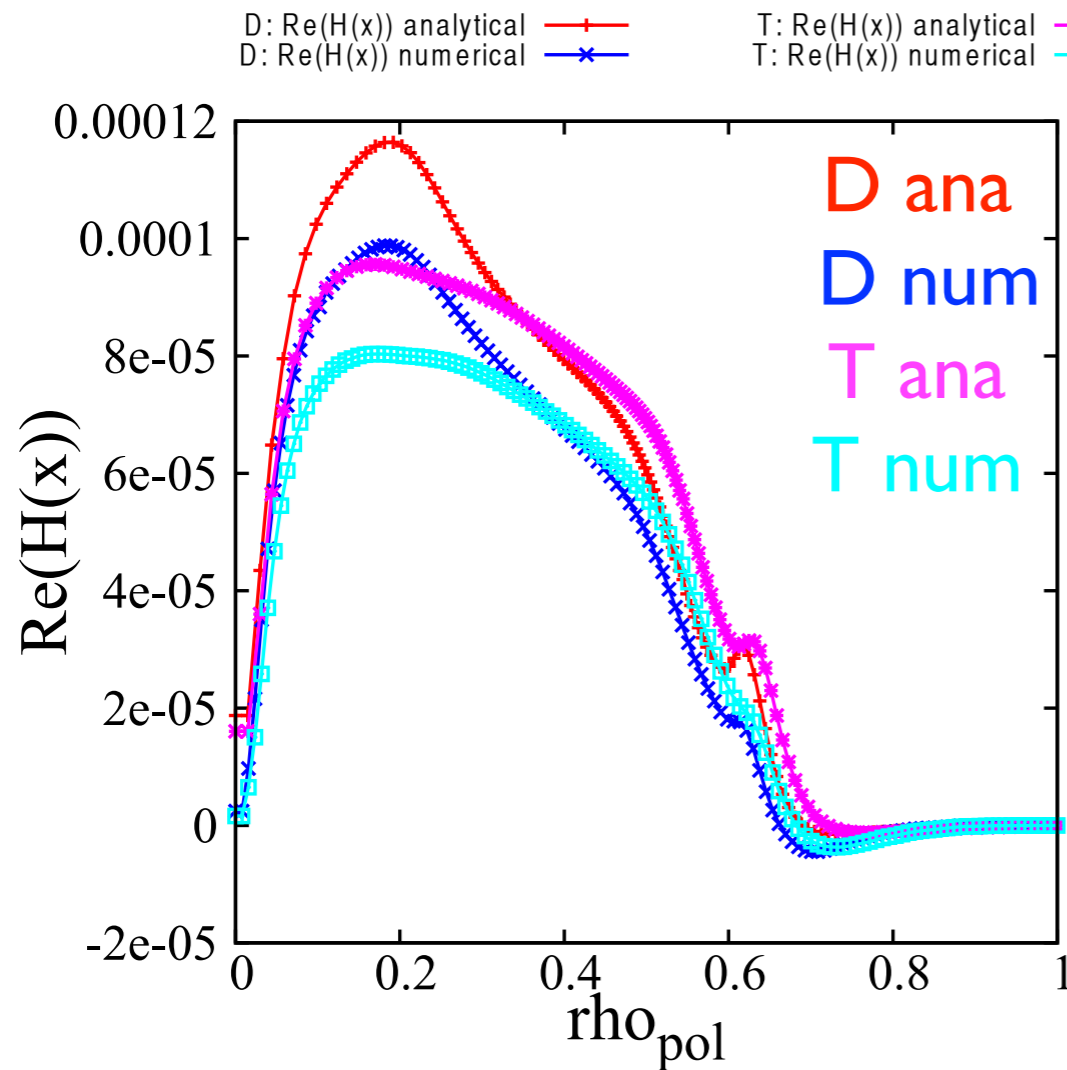
$$\begin{aligned}
 & - \frac{\partial}{\partial t} \left[\nabla \cdot \frac{1}{v_A^2} \nabla_{\perp} \phi \right] + \mathbf{B} \cdot \nabla \frac{\nabla \times (\nabla \times (\frac{\nabla \psi}{i\omega})_{\parallel} \mathbf{b})}{B} + (\mathbf{b} \times \nabla (\frac{\nabla \psi}{i\omega})_{\parallel} \mathbf{b}) \cdot \nabla \frac{\mu_0 j_{\parallel}}{B} \\
 & = - \sum_a \mu_0 \int d^2v e_a \{v_{\perp} \cdot \nabla J_0 f\}_a + \sum_a \left[\mathbf{b} \times \nabla \left(\frac{\beta_{a\perp}}{2\Omega_a} \right) \right] \cdot \nabla \nabla_{\perp}^2 \phi \\
 & + \sum_a \frac{3v_{th,a}^2}{8v_A^2 \Omega_a^2} \nabla_{\perp}^4 \frac{\partial \phi}{\partial t} + \mathbf{B} \cdot \nabla \frac{1}{B} \sum_a \frac{\beta_a}{4} \nabla_{\perp}^2 (\frac{\nabla \psi}{i\omega})_{\parallel} \mathbf{b} \quad \text{GKM}
 \end{aligned}$$

$$\begin{aligned}
 \hat{h} &= ie \sum_m \int_{-\infty}^t dt' e^{i[n(\varphi' - \varphi) - m(\theta' - \theta) - \omega(t' - t)]} e^{-im\theta} \\
 & \frac{\partial F_0}{\partial E} [\omega - \omega_*] J_0(k_{\perp} \rho_i) \left[\phi_m(r') - \left(1 - \frac{\omega_d(r', \theta')}{\omega}\right) \psi_m(r') \right] \quad \text{GKE}
 \end{aligned}$$

$$f = h + H_1 \frac{\partial F_0}{\partial E} - \left[e \frac{\partial F_0}{\partial E} - \frac{c \nabla F_0}{i\omega B} \cdot (\mathbf{b} \times \nabla) \right] J_0 \psi,$$



comparison analytical theory - numerical integration; can be calculated including FLR/FOW effects (100 times faster!)



- similar dependence for analytical expression vs numerical result
- D and T damping differ - exponential dependence of ion LD!
- numerical damping is typically smaller than analytical expression (assumption $v=v_{||}$)

$v_{th,e}/v_{A0}$	~ 13
$v_{th,D}/v_{A0}$	~ 0.2
$v_{th,T}/v_{A0}$	~ 0.16
$v_{th,He}/v_{A0}$	~ 0.14
$v_{th,Be}/v_{A0}$	~ 0.09