

# Non-linear ELM and RMP Modeling in Realistic Tokamak Geometries

A diagram showing a cross-section of a tokamak plasma. The plasma is represented by a central yellow and orange region, surrounded by a green and blue region, all contained within a red and pink outer boundary. The diagram is overlaid with a grid of colored lines, suggesting a simulation or modeling process.

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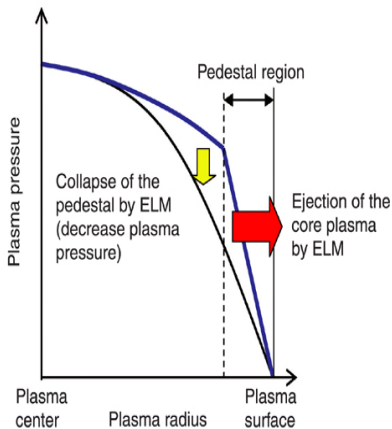
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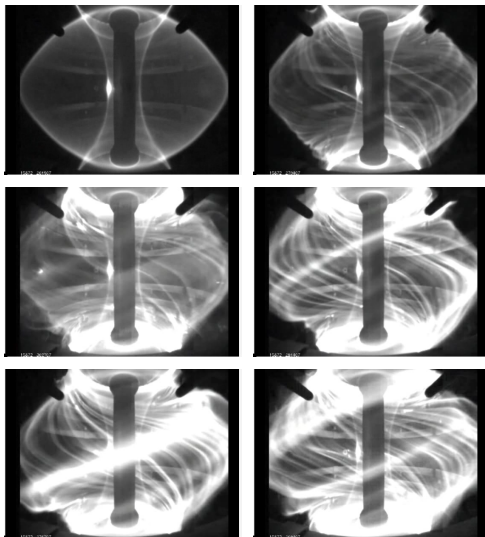
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<sup>5</sup>EURATOM/CCFE Association, Culham Science Centre, UK



MAST fast CCD camera

[Kirk '06]



**Periodic relaxation of heat & density**

↳ steep  $\nabla p$  (ballooning)

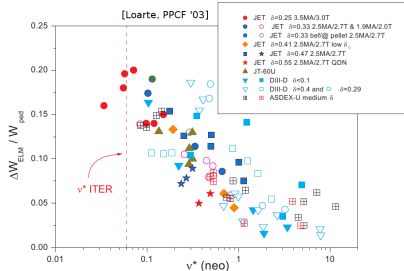
↳ large edge current (peeling)

## Limits pedestal height & global confinement

- ▶ erosion, droplets, melting of tungsten
- ▶  $Q=10$  in ITER:  $\Delta W_{ELM}^{ITER} \sim 17\text{MJ} \sim 15\% W_{ped}$   
[in  $\sim 250\text{-}500 \mu\text{s}$ ]
- ▶ **acceptable ELM**:  $\Delta W_{ELM} \sim 2 - 3\text{MJ}$   
↳ divertor may only survive a few ELMs. . .

- ▶  $e^-$  gun power load based on **empirical extrapolation** —not understood
- ▶ power load cycles ( 1000) at low power show intense material degradation

ELMy power load:  $e^-$  gun @Kurchatov



## Limits pedestal height & global confinement

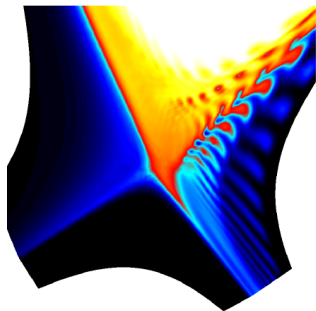
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**Common thread:** what requirements for an accurate description of ELMs & RMPs?

1. the tool: the reduced MHD code JOREK
2. evaluating the ELM energy deposition in ITER
3. added physics: diamagnetics & RMPs
4. going further: divertor physics



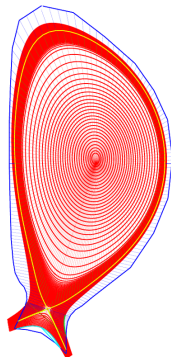
## Requirements for an accurate description of ELMs & RMPs

- 1 the tool: the reduced MHD code JOEAK
- 2 The ELM energy deposition in ITER
- 3 Added physics: diamagnetics & RMPs
- 4 Going further: divertor physics

- ▶ Originally developed at CEA Cadarache [Huijsmans '07, Czarny '08]
- ▶ Non-linear reduced MHD in toroidal geometry  
[*next slide: dens., temp., elec. potential (perp. flow), para. velocity, polo. flux*]
- ▶ Full MHD in development

[see A. Ratnani, tomorrow]

- Domain:
    - Closed & open field lines, X-point
    - b.c.: Mach one, free outflow at divertor target
  - Discretisation:
    - Cubic Bezier finite elements in the poloidal plane
    - Fourier series in toroidal angle
  - Time stepping: fully implicit Crank-Nicholson
  - Solver sparse matrices (PastiX library):  $10^7$  degrees of freedom
  - Parallelisation using MPI/OpenMP: typically 256 – 1500 processors
- 
- ▶ Pellet ELM triggering [Huijsmans '10]
  - ▶ ELMs in JET [Pamela '11]
  - ▶ RMP field penetration [Bécoulet '12, Orain '13]



**1—density:** 
$$\frac{\partial}{\partial t} \rho = -\nabla \cdot (\rho \mathbf{v}) + \nabla \cdot (D_\perp \nabla_\perp \rho) + S_\rho$$
 [Huijsmans '09, Orain '13]

**2—temperature:** 
$$\rho \frac{\partial}{\partial t} T = -\rho \mathbf{v} \cdot \nabla T - (\gamma - 1) \rho T \nabla \cdot \mathbf{v} + \nabla \cdot (\kappa_\perp \nabla_\perp T + \kappa_\parallel \nabla_\parallel T) + S_T$$

**3—perp. and parallel momentum:**

$$\mathbf{e}_\varphi \cdot \nabla \times \left( \rho \frac{\partial}{\partial t} \mathbf{v} = -\rho (\mathbf{v} \cdot \nabla) \mathbf{v} - \nabla (\rho T) + \mathbf{J} \times \mathbf{B} + \mu \Delta \mathbf{v} - \nabla \cdot \Pi^{neo} + S_{v_\varphi} \right)$$

$$\mathbf{B} \cdot \left( \rho \frac{\partial}{\partial t} \mathbf{v} = -\rho (\mathbf{v} \cdot \nabla) \mathbf{v} - \nabla (\rho T) + \mathbf{J} \times \mathbf{B} + \mu \Delta \mathbf{v} - \nabla \cdot \Pi^{neo} + S_{v_\varphi} \right)$$

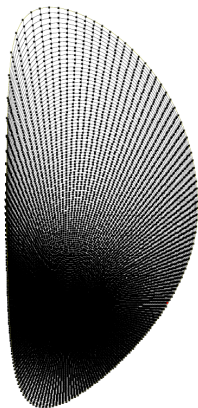
**5—induction:** 
$$\frac{\partial}{\partial t} \mathbf{A} = -\eta \mathbf{J} - \frac{m}{\rho e} \nabla_\parallel (\rho T) + \mathbf{v} \times \mathbf{B} - F_0 \nabla \phi$$

**6—B field & closure:**

$$\mathbf{B} = \frac{F_0}{R} \mathbf{e}_\varphi + \frac{\nabla \psi(t)}{R} \times \mathbf{e}_\varphi \quad ; \quad \eta = \eta_0 (T/T_0)^{-3/2} \quad ; \quad \mathbf{v} = -R \nabla \phi(t) \times \mathbf{e}_\varphi + v_\parallel(t) \mathbf{B} + \mathbf{v}_*$$

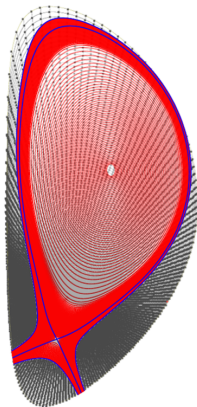
**7—boundary conditions:**

- ▶ Zero perturbations on wall aligned with last flux surface
- ▶ Bohm boundary conditions on the target:  $v_\parallel = \pm c_s$  ;  $\kappa_\parallel \mathbf{b} \cdot \nabla T = (\gamma - 1) n T c_s$

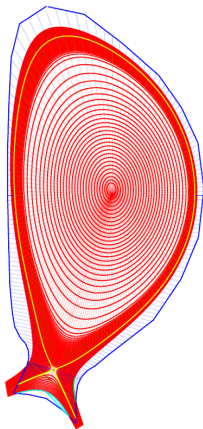


- ▶ Initial grid: polar grid for Bézier elements
- ▶ Flux-aligned grid including X-point(s)
- ▶ Radial and poloidal grid meshing: divertor & wall b.c.
- ▶ Equilibrium flows:  $n = 0$  harmonic
- ▶ Time-integration:  $\forall n$  harmonics
- ▶ Postprocessing

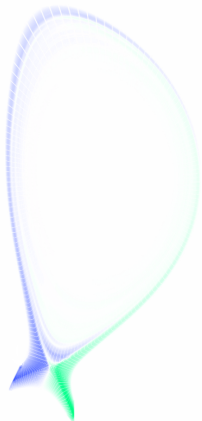




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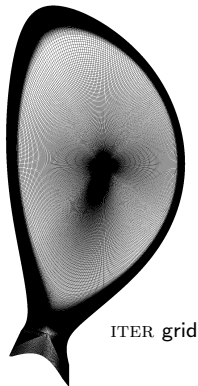
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③ Added physics: diamagnetics & RMPs

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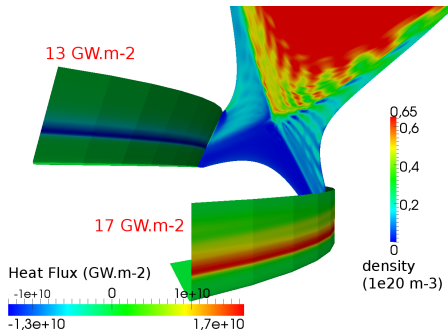
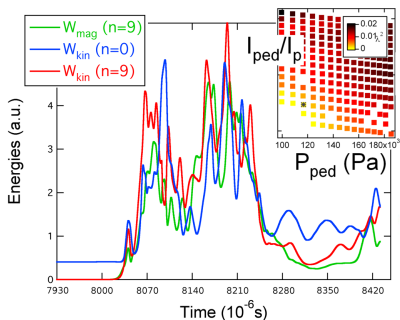
F4E-GRT265:

« Evaluation of edge MHD stability and uncontrolled ELM energy losses for ITER H-mode plasmas in non-active, DD and DT operational scenarios »

↳ known limitations ➡ a realistic ELM computation in ITER is yet out-of-scope

state-of-the-art: preliminary attempt to compute heat & particle deposition in 15MA/5.3T ITER

[Maget '12, Dif-Pradalier & Bécoulet '13]



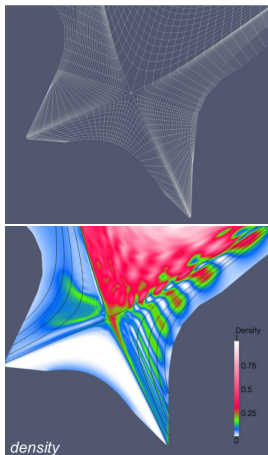
- ▶ **particle loss in ELM:**  $\sim 3.4\%$
- ▶ **energy loss in ELM:** 5MJ out of 452.5MJ  $\sim 1.1\%$  energy content

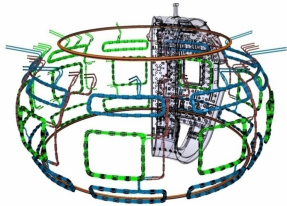
Resistivity	$\eta_0 = 10^{-6}$	$10^{-10}$
Parallel/perp. heat cond.	$\kappa_{\parallel} / \kappa_{\perp} = 810^8$	$10^{11}$

going beyond. . .

- **grid:**
  - aligned v.s. adaptive [Ratnani]
  - low  $\eta_0 \Rightarrow$  large grid  $\Rightarrow$  memory
- **memory:** multi-harmonics needed for turb. &  $\mathbf{E} \times \mathbf{B}$  shear  $\Rightarrow$  large in implicit models
- **time-stepping:** fast parallel dyn. v.s. perp.
- **boundaries:** interaction with chamber magn. connection, free boundary [STARWALL]

$\Rightarrow$  how does the ELM computation change when adding new physics?





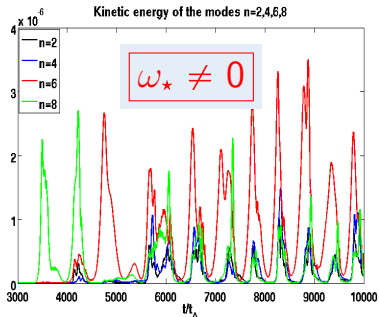
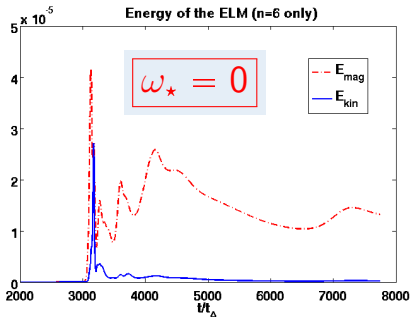
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## why a cycle?

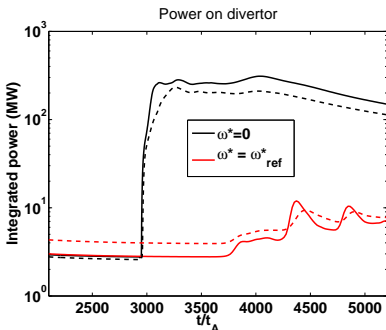
- usually: initial unstable profiles  $\nabla p$ ,  $I$   $\Rightarrow$  single relaxation
- 1<sup>st</sup> relax.: “unphysical” ?  $\Rightarrow$  analog. sawteeth [q-profile, reconn. dyn.] [Lütjens '09]
- assess dynamics with self-consistent background flows, electric field & mode phasing



[Orain '13]

- ▶ when including dia. rotation...

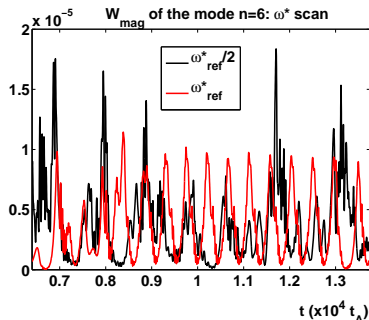
↳ heat deposited on divertor is  
reduced when  $\omega_* \neq 0$



[Orain '13]

- ▶ ELM freq. ↗ when  $\omega_*$  ↘

↳ ELM size & dynamics ⇒ 2-fluid  
dia. rotation important



External coils apply static Resonant Mag. Perturb.

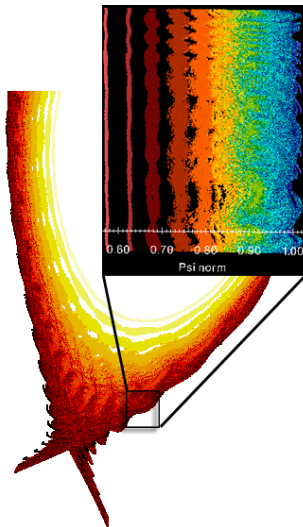
ergodic edge

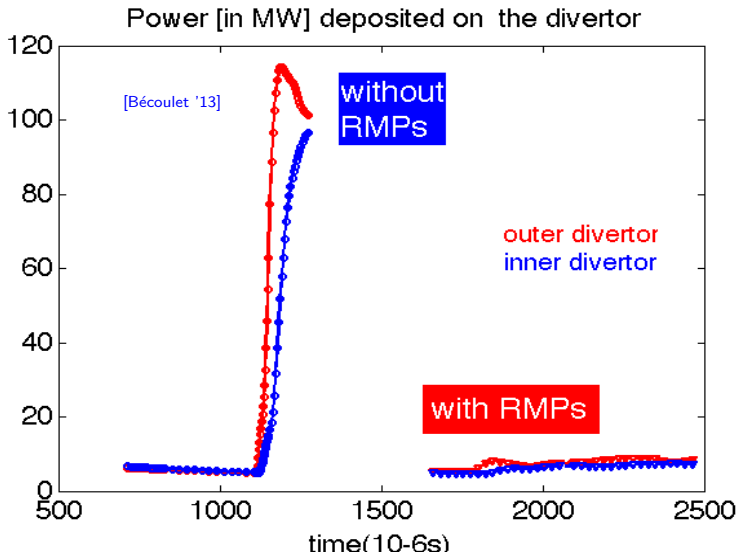
radial transport ↗

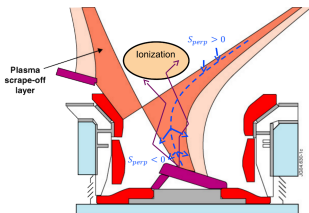
$\nabla p \searrow < \text{instability threshold}$

- ▶ same “vacuum ergodization”, different effects: **suppress, mitigate, trigger,...**

- RMPs with plasma response
- RMPs / ELMs interaction
- Density pump-out
- Rotation braking





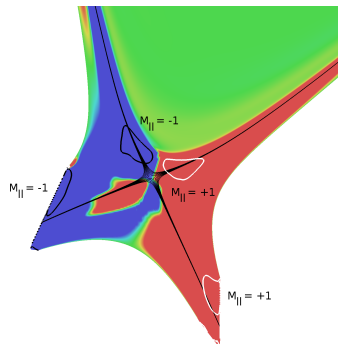


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- ▶ Flows  $\implies$  strong influence on onset & development of instabilities [see  $\omega_*$ ]  
 ↳ **supersonic transitions** in JOEUK: a surprise?
- ▶  $\{S, \text{neutrals, geom.}\}$   $\implies$  strong influence on onset & structure of flows

Supersonic transition in the SOL driven by plasma source inversion



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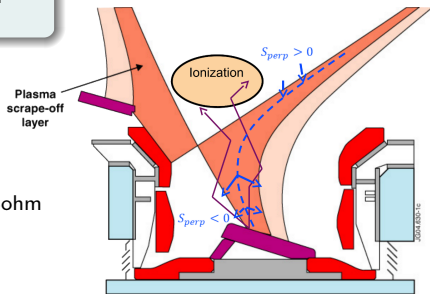
Supersonic transition in the SOL driven by plasma source inversion

$$\mathcal{A} = \frac{2M}{1+M^2} \quad [\text{Ghendrih '12, Bufferand '13}]$$

$$\frac{\partial \mathcal{A}}{\partial S} \propto (S_{\text{perp}} + S_{\text{ionization}})$$

■ If  $\partial_S \mathcal{A} \leq 0$  target plates  $\Rightarrow M \geq 1$  satisfy Bohm

■  $\underbrace{S_{\text{perp}} + S_{\text{ioniz.}}}_{\text{near target plates}} \left. \begin{array}{l} < 0 \Rightarrow \text{supersonic} \\ > 0 \Rightarrow \text{subsonic} \end{array} \right\}$



**supersonic flows**

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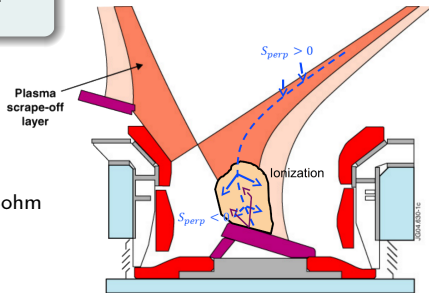
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**NO supersonic flows**



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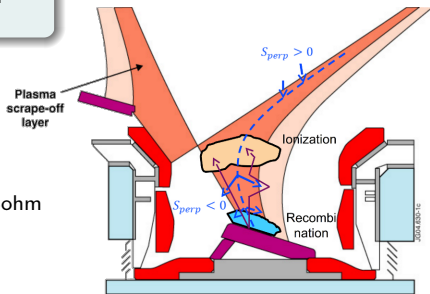
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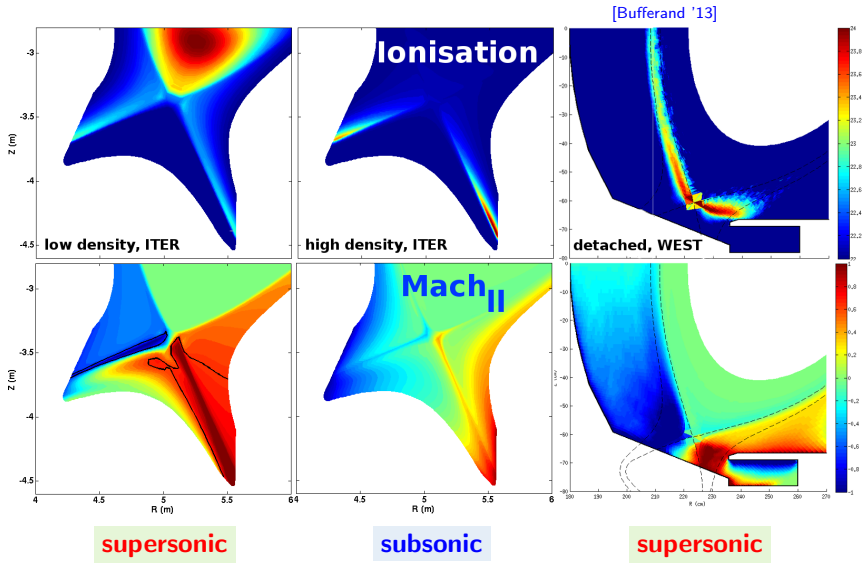
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**supersonic flows**



First series of ELM computation for iter [ $0^{th}$  order], validated by ITER.

Diamagnetic flows  $\omega_*$ :

- seem essential for ELM cycles
- reduce ELM size, increase freq.
- symmetrisation of the power deposition

ELM mitigation by RMPs

Supersonic flow transitions in SOL —divertor physics

- framework understanding becoming mature
- delicate balance: sources, neutrals [ionis.],  $\mathbf{B}$  geom.  $\Rightarrow$  all effects important

many numerical challenges remain, *e.g. talk tomorrow by A. Ratnani*

# Additional material

## ▶ non-linear reduced MHD in toroidal geometry

- density, temperature, velocity & poloidal flux
- ideal wall conditions on walls
- Mach one, free outflow at divertor target

## ▶ closed & open field lines domain, X-point geom.

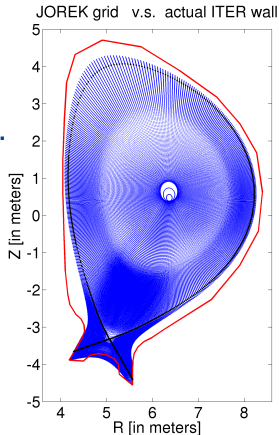
- cubic finite elements, flux aligned poloidal grid
- Fourier series in toroidal direction

## ▶ time stepping, solver & parallelism

- fully implicit Crank-Nicholson
- sparse matrices (PASTIX):  $\sim 10^7$  degrees of freedom
- MPI/OpenMP over typically 256 – 1500 processors

## ▶ getting closer to the experiment...

- exact **geometry**\*\* & **boundary conditions**\*\*
- non-linear MHD over **long time scales**\* ( $\mu s \rightarrow s$ )
- **realistic parameters**\*\*\* [resistivity, parallel conductivity, collisionality]
- **one/several modes**\*\*\*, background **turbulence**\*\*\*\*



## ▶ ELM cycle & control

- ELMs [G. Dif-Pradalier, M. Bécoulet, S. Pamela]
- Resonant Magnetic Perturbations (RMPs) [M. Bécoulet, F. Orain]
- pellets injection, vertical kicks [G. Huijsmans, S. Futatani]

## ▶ Disruptions

- VDE,  $\beta$  limit disruptions, density limit [C. Reux, E. Nardon, A. Fil]
- NTMs control with ECCD [IO+FOM]

**ANRs:** ASTER (2006-2009), ANIKA (2009-2012), ANEMOS (2010-2013), A2T2 (2010-2013)

**Grants:** F4E-2011-GRT-265

“Jorek team”: ~ 30 throughout Europe

international:		JOREK	[Huijsmans '07]
		M3D-C1	[Ferraro '09]
		XGC0	[Park '07]
		BOUT++	[Dudson '09]

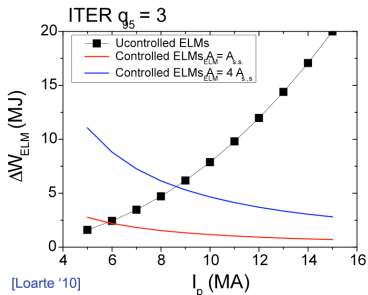
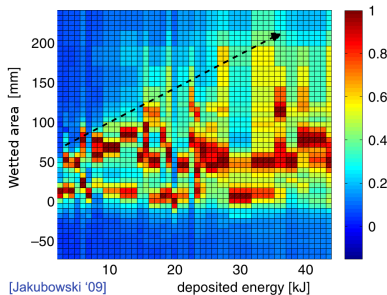


ELM  $\equiv$  MHD instability destabilised by pressure & current gradients in the H-mode pedestal

▶ stringent operational limits:  $W_{ELM}/W_{ped} \sim 15\%$  in  $\sim 250\text{-}500 \mu\text{s}$

3 major players:

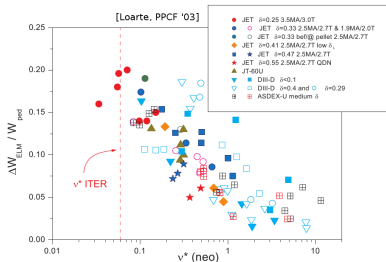
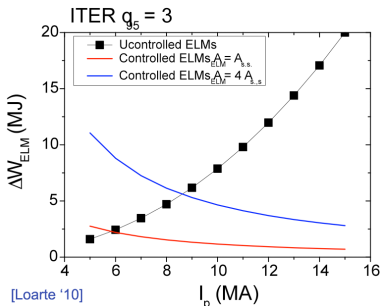
- **ELM energy content:**  $W_{ELM} \nearrow$  when coll.  $\searrow$  [Loarte '03, Pamela '10, Zarzoso '11]
- **ELM energy deposition area:** does the power density  $\nearrow$  when  $W_{ELM} \nearrow$ ?  
wetted area during ELM increase with ELM size
- **peak heat load localisation:** changes during ELM [Thomsen '10]



Gr#265  $\equiv$  study these aspects in realistic iter geometry and standard [15MA, 6keV] scenario

[ELM power loads: conservative ; broadening not taken into account]

- ▶ Uncontrolled ELMs in ITER :  $\sim 20\text{MJ}$  at  $15\text{MA}$ ,  $Q = 10$ 
  - ▶ acceptable limit for material damage :  $0.5 \text{ MJ m}^{-2}$ ,  $\Delta W_{ELM}^{contr.} \sim 0.7 \text{ MJ}$
- ▶ A significant broadening of ELM footprint could increase uncontrolled ELM operation from  $6\text{MA}$  ( $A_{ELM} = A_{SS}$ ) to  $9\text{MA}$  ( $A_{ELM} = 4A_{SS}$ )
  - ▶ No large influence on ELM size limit at  $15\text{MA}$  (small ELMs)

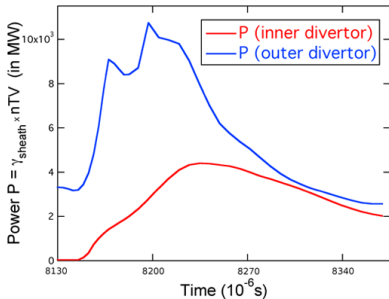


## Ongoing effort: assess energy & particle deposition for Iter

- ▶ realistic parameters challenging:  $\nu_*$ , resistivity  $\eta$ , transp. anisotropy  $\chi_{\parallel}/\chi_{\perp}$ , size, shape...



- ▶ **particle loss in ELM:**  $\sim 3.4\%$
- ▶ **energy loss in ELM:** 5MJ out of 452.5MJ  $\sim 1.1\%$  energy content
- ▶ near-symmetric power deposition for a large ELM



Resistivity	$\eta_0 = 10^{-6}$	$10^{-10}$
Parallel/perp. heat cond.	$\kappa_{\parallel} / \kappa_{\perp} = 810^8$	$10^{11}$

Diamagnetics	none
Neoclassics	none
Neutrals	none
Radiation	none
Harmonics	single [ $n = 9$ ]
ELM cycle	single relax.

➡ what happens when relaxing some of the above limitations ?